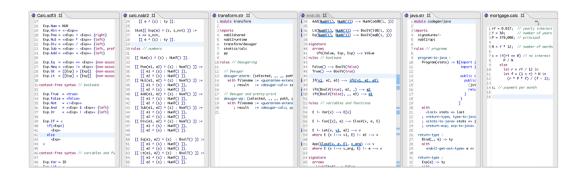
Safety and Completeness of Disambiguation corresponds to Termination and Confluence of Reordering

Eelco Visser

Joint work with Eduardo Amorim

June 30, 2020
International Workshop on Confluence (IWC'20)
Co-located with FSCD and IJCAR
'Paris, France'

Spoofax Language Workbench









DynSem: Dynamic Semantics



Stratego: Program Transformation



Programming Environment

Syntax Definition in Spoofax

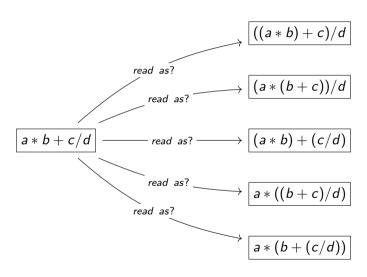
Many syntactic (editor) services from single declarative syntax definition

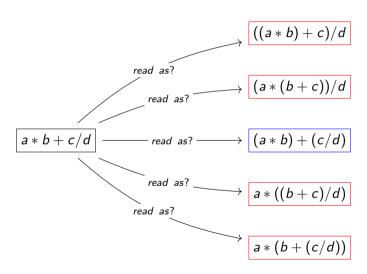
```
lexical syntax
  ID = [a-zA-Z][a-zA-Z0-9]*
context-free syntax
  Exp.Var = <<ID>>
  Exp.Add = <<Exp> + <Exp>> {left}
  Exp.Mul = <<Exp> * <Exp>> {left}
context-free priorities
  Exp.Mul > Exp.Add
```

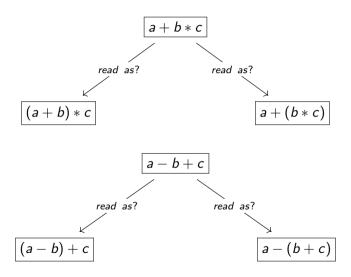
- syntax checking
- error recovery
- syntax highlighting
- abstract syntax
- formatting
- syntactic completion
- parenthesis insertion
- declarative disambiguation

History

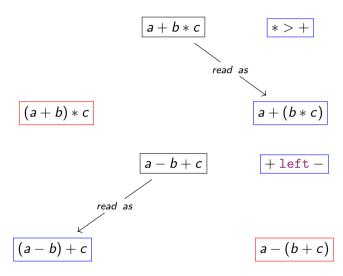
- 1997 My PhD thesis with semantics of disambiguation rules for SDF2
- 2011 Peter Mosses observes unsafety of SDF2 rules
- 2013 Afroozeh et al. (SLE'13) define safe disambiguation with grammar transformation; semantics in terms of derivations; no proof of correctness
- 2018 First submission to TOPLAS and implementation of new parser generator for SDF3 integrated in Spoofax
- 2019 Chapter in PhD thesis Eduardo Amorim and major revision for TOPLAS: safe and complete semantics based on subtree exclusion with proof (sketch)
- 2020 Work in progres: TOPLAS 'minor' revision with new approach to proof of safety and completeness

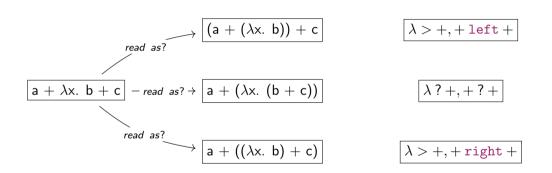






Associativity and Priority





In this talk:

- ▶ What is the semantics of associativity and priority rules?
- Is a set of disambiguation rules safe?
- Is a set of disambiguation rules complete?
- ► How to prove that?

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Not in this talk:

- ▶ What classes of ambiguities do associativity and priority rules solve?
- What is an effective implementation strategy for disambiguation rules?

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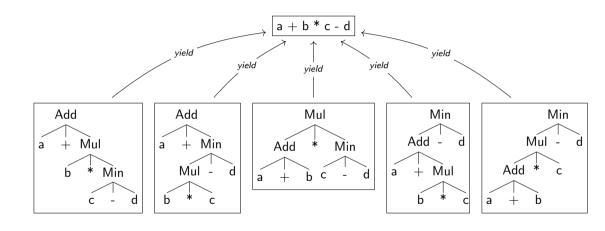
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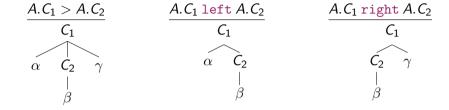
Why is this not a solved problem?

- ▶ Ambiguity of context-free grammars is undecidable; why bother?
- Existing definitions depend on specific implementations

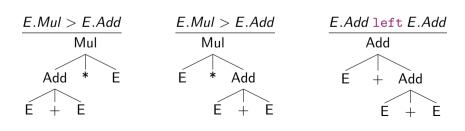
Ambiguous Sentence has Multiple Parse Trees



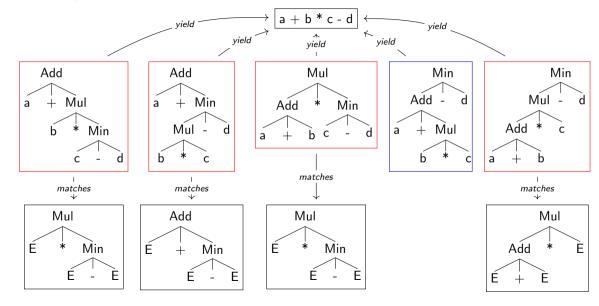
Associativity and Priority as Subtree Exclusion Rules [SDF2 (1997)]



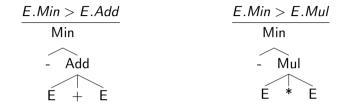
Disambiguation rules generate subtree exclusion patterns (aka conflict patterns)

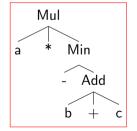


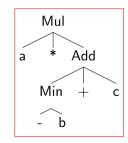
Disambiguation by Subtree Exclusion

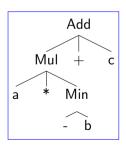


Safe for High Priority Prefix Operators

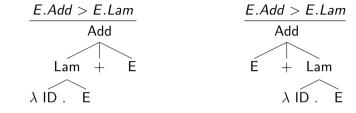


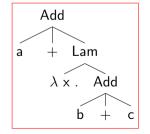


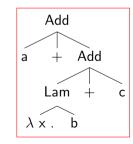


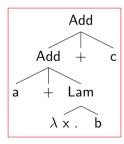


Unsafe for Low Priority Prefix Operators [SDF2]

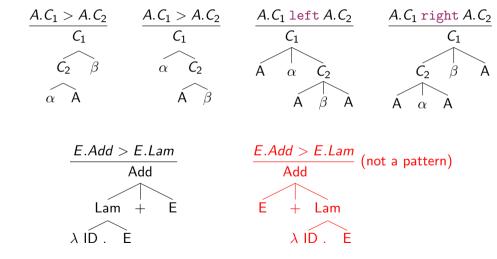




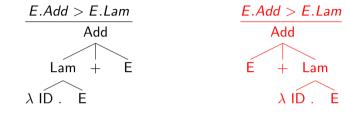


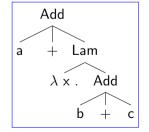


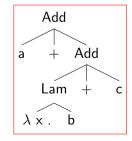
Safe Subtree Exclusion Rules [SDF3 (2019)]

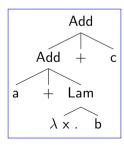


Shallow Interpretation: Safe for Low Priority Prefix Operators

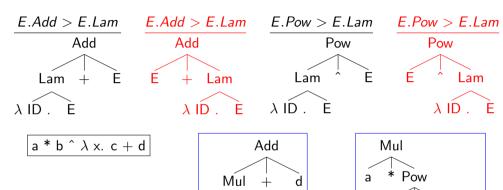


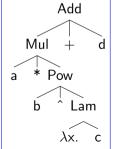


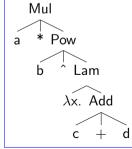




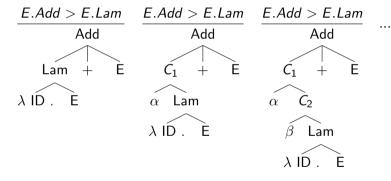
Shallow Interpretation: Incomplete for Low Priority Prefix Operators

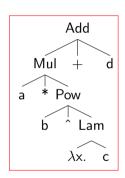






Deep Priority Conflicts: Match Subpattern in Right-Most Subtree



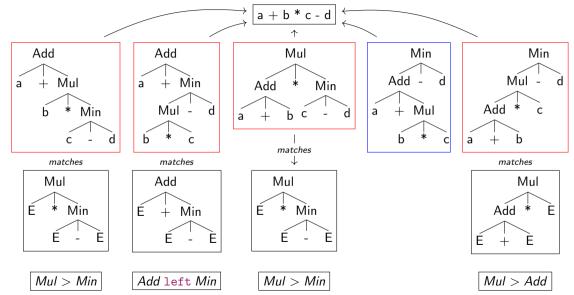


Infinite set of conflict patterns

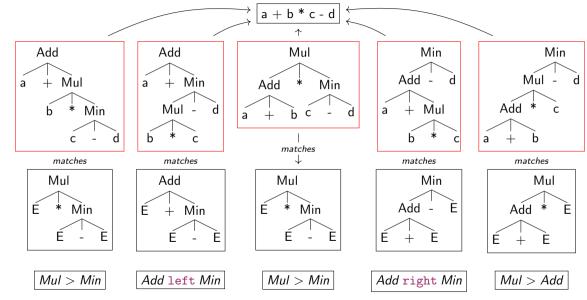
- √ What is the semantics of associativity and priority rules?
 - ▶ Integrated in implementation of SDF3 parser generator
 - ► Has been available since 2018 in Spoofax
- Is a set of disambiguation rules safe for a particular grammar?
- Is a set of disambiguation rules complete for a particular grammar?
- How to prove that?

Restricting to the case of infix expression grammars for this talk.

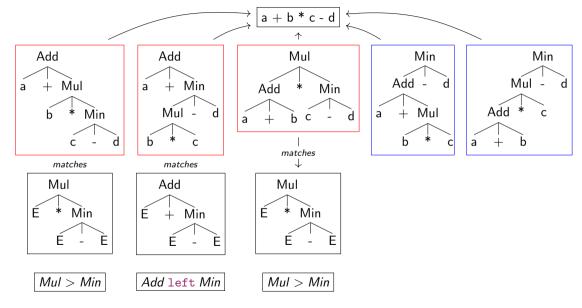
Safe and Complete Disambiguation Rules



Unsafe: Too Many Disambiguation Rules



Incomplete: Too Few Disambiguation Rules



- √ What is the semantics of associativity and priority rules?
- √ Is a set of disambiguation rules safe for a particular grammar?
 - At most one rule for each pair of productions
 - ► + some well-formedness criteria
- √ Is a set of disambiguation rules complete for a particular grammar?
 - At least one rule for each pair of productions
 - + some well-formedness criteria
- How to prove that?

Trees under Subtree Exclusion

Definition

A tree $t \in T^Q(G)$ iff $t \in T(G)$ and no subtree of t matches a conflict pattern in Q.

Lemma (Safety)

A disambiguation relation is safe, if for each $w \in L(G)$ there is at least one tree $t \in T^Q(G)$ such that yield(t) = w.

Lemma (Completeness)

A disambiguation relation is complete, if for each $w \in L(G)$ there is at most one tree $t \in T^Q(G)$ such that yield(t) = w.

To prove safety:

If a tree $t \in T(G)$ has a conflict, then there is another tree for the same sentence that does not have a conflict.

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To prove completeness:

If a tree $t \in T(G)$ does not have a conflict, then all other trees for the same sentence have conflicts.

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Subtree exclusion is a statement about a single tree

How do we relate all trees for the same sentence?

To prove safety:

If a tree $t \in T(G)$ has a conflict, then there is another tree for the same sentence that does not have a conflict.

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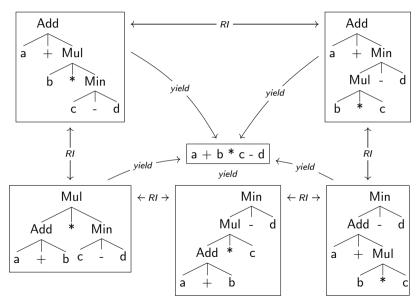
Subtree exclusion is a statement about a single tree

How do we relate all trees for the same sentence?

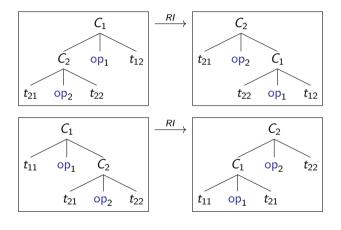
The solution is simple and elegant; once you have seen it you can't unsee it; but for the longest time I didn't see it (nor did co-authors, reviewers, other readers)*.

^{*} But Haskell infix operators are implemented using such reorderings

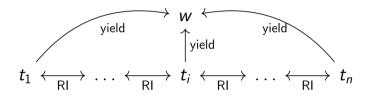
Insight: Trees for Ambiguous Sentence are Reorderings



Reordering Rewrite System

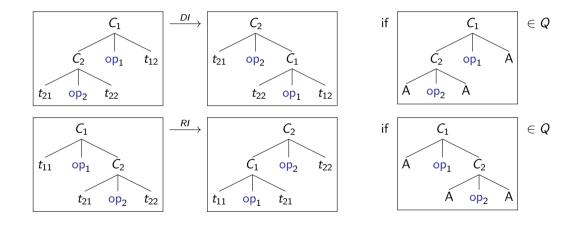


Theorem: Infix Ambiguities are Reorderings

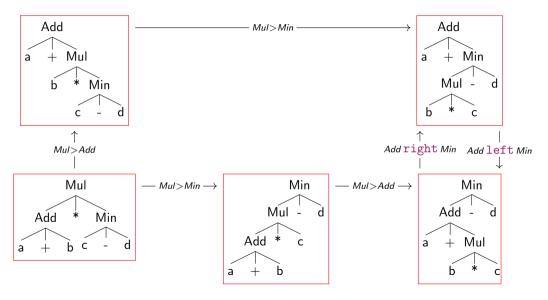


Fine print: for expression grammars beyond infix expression grammars, there are some extra requirements.

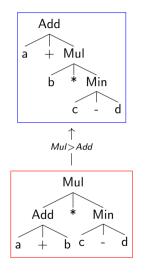
Ordering Reorderings with Conflict Patterns

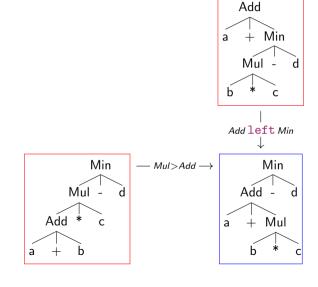


Correspondence: Unsafety is Non-Termination

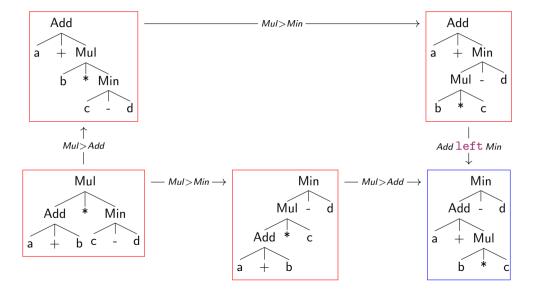


Correspondence: Incompleteness is Non-Confluence (Non-Church Rosser)





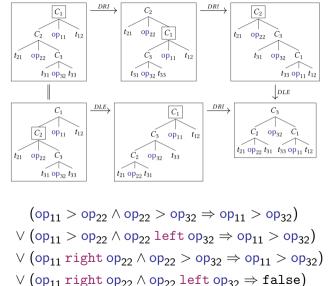
Correspondence: Safety + Completeness is Termination + Confluence



Proving Termination and Completeness

- ► Termination = Safety
 - A safe disambiguation relation induces a reduction order on DI
 - Roughly: number of conflicts reduces to zero
- Confluence = Completeness
 - ▶ If disambiguation relation is complete, then DI is locally confluent
 - ► DI (infix) has 5 critical pairs
 - ► The conditions for the rules in a critical pair + well-formedness criteria on disambiguation relation enable other rules and completion of the diagram
 - Extension with prefix and postfix operators: 8 rules, 28 critical pairs, 36 cases.
 - Automated by implementation in Stratego

Proving Local Confluence: Critical Pairs are Joinable



- √ What is the semantics of associativity and priority rules?
- ✓ Is a set of disambiguation rules safe for a particular grammar?
 - At most one rule for each pair of productions
 - + some well-formedness criteria
- √ Is a set of disambiguation rules complete for a particular grammar?
 - At least one rule for each pair of productions
 - + some well-formedness criteria
- √ How to prove that?
 - Disambiguation corresponds to reordering conditional on conflict patterns
 - Trees under subtree exclusion: normal forms of DI
 - Safety of disambiguation
 - DI is terminating iff disambiguation relation is safe
 - Completeness of disambiguation
 - ▶ DI is confluent iff disambiguation relation is complete

What Else?

- ▶ What clasess of ambiguities do associativity rules solve?
 - ▶ Short answer: expression grammars for which ambiguities correspond to reorderings
 - We have investigated several classes of expression grammars: prefix/postfix operators, mixfix grammars, dangling suffix/prefix, indirect recursion, longest match of lists
- ▶ What happened to the undecidability of ambiguity?
 - Expression grammars without overlap: ambiguities are reorderings
 - Infix grammars: cannot have overlap
 - ► IPP grammars: harmful overlap is decidable (conjecture)
 - Mixfix grammars: harmful/less overlap undecidable in general
 - ▶ But: need only inspect productions involved in overlap
- ▶ What is an effective implementation strategy for disambiguation rules?
 - Contextual grammar transformations
 - Data dependent parsing
- ► A full paper is underway
 - ► A Direct Semantics for Declarative Disambiguation of Expression Grammars
 - Under revision for ACM TOPLAS